MA 114 Worksheet #04: Integration by partial fractions

1. Write out the general form for the partial fraction decomposition but do not determine the numerical value of the coefficients.

(a)
$$\frac{1}{x^2 + 3x + 2}$$

(b) $\frac{x+1}{x^2 + 4x + 4}$
(c) $\frac{x}{(x^2 + 1)(x+1)(x+2)}$
(d) $\frac{2x+5}{(x^2 + 1)^3(2x+1)}$

- 2. Based on your work in the previous question, can you conjecture (guess) a relation between the degree of the denominator of the rational function and the number of coefficients in the partial fraction decomposition?
- 3. Find the partial fraction decomposition for the following rational functions.

4. Compute the following integrals.

(a)
$$\int \frac{x-9}{(x+5)(x-2)} dx$$

(b) $\int \frac{1}{x^2+3x+2} dx$
(c) $\int \frac{x^3-2x^2+1}{x^3-2x^2} dx$
(d) $\int \frac{x^3+4}{x^2+4} dx$
(e) $\int \frac{1}{x(x^2+1)} dx$

5. Compute

$$\int \frac{1}{\sqrt{x} - \sqrt[3]{x}} \, dx$$

by first making the substitution $u = \sqrt[6]{x}$.